

Chiralità legata all'operatore

$$\gamma^5 = i\gamma^0\gamma^1\gamma^2\gamma^3 \quad (\gamma^5)^2 = \mathbb{I} \quad (\gamma^5)^\dagger = \gamma^5 \quad \gamma^5\gamma^\mu = -\gamma^\mu\gamma^5 \quad (9)$$

Proiettori di chiralità

$$P_R = \frac{1}{2}(1 + \gamma^5) \quad P_L = \frac{1}{2}(1 - \gamma^5) \quad (10)$$

$$\psi_R = P_R \psi \quad \psi_L = P_L \psi$$

Sono autostati di γ^5

$$\gamma^5 \psi_R = \gamma^5 \frac{1}{2}(1 + \gamma^5) \psi = \frac{1}{2}(\gamma^5 + \mathbb{I}) \psi = \psi_R \quad (11a)$$

$$\gamma^5 \psi_L = \gamma^5 \frac{1}{2}(1 - \gamma^5) \psi = \frac{1}{2}(\gamma^5 - \mathbb{I}) \psi = -\psi_L \quad (11b)$$

ψ_R e ψ_L non sono autostati di m .

$$i\gamma^\mu \frac{\partial}{\partial x^\mu} \psi_R = i\gamma^\mu \frac{\partial}{\partial x^\mu} \left[\frac{1}{2}(1 + \gamma^5) \psi \right] = \frac{1}{2} \gamma^\mu \frac{\partial \psi}{\partial x^\mu} + \frac{1}{2} \gamma^\mu \gamma^5 \frac{\partial \psi}{\partial x^\mu}$$

$$= \frac{1}{2} \gamma^\mu \frac{\partial \psi}{\partial x^\mu} - \frac{1}{2} \gamma^5 \gamma^\mu \frac{\partial \psi}{\partial x^\mu} = \frac{1}{2}(1 - \gamma^5) \gamma^\mu \frac{\partial \psi}{\partial x^\mu} =$$

$$= \frac{1}{2}(1 - \gamma^5) m \psi = m \frac{1}{2}(1 - \gamma^5) \psi = m \psi_L \quad (12)$$

Viceversa per ψ_L

$$i\gamma^\mu \frac{\partial}{\partial x^\mu} \psi_L = m \psi_R \quad (13)$$