

$$iG^0(\vec{x}t, \vec{x}'t') = \sum_{\vec{k}\vec{k}'} \phi_{\vec{k}}(\vec{x}) \phi_{\vec{k}'}^*(\vec{x}') e^{-i\omega_{\vec{k}}t} e^{i\omega_{\vec{k}'}t'} \langle \bar{\Phi}_0 | a_{\vec{k}} a_{\vec{k}'}^\dagger | \bar{\Phi}_0 \rangle \vartheta(t-t') \\ - \sum_{\vec{k}\vec{k}'} \phi_{\vec{k}}(\vec{x}) \phi_{\vec{k}'}^*(\vec{x}') e^{-i\omega_{\vec{k}}t} e^{i\omega_{\vec{k}'}t'} \langle \bar{\Phi}_0 | a_{\vec{k}'}^\dagger a_{\vec{k}} | \bar{\Phi}_0 \rangle \vartheta(t'-t)$$

$$\langle \bar{\Phi}_0 | a_{\vec{k}} a_{\vec{k}'}^\dagger | \bar{\Phi}_0 \rangle = \delta_{\vec{k}\vec{k}'} \vartheta(k - k_F)$$

$$\langle \bar{\Phi}_0 | a_{\vec{k}}^\dagger a_{\vec{k}'} | \bar{\Phi}_0 \rangle = \delta_{\vec{k}\vec{k}'} \vartheta(k_F - k)$$

$$\phi_{\vec{k}}(\vec{x}) = e^{-i\vec{k}\vec{x}} \frac{1}{\sqrt{V}}$$

$$iG^0(\vec{x}t, \vec{x}'t') = \frac{1}{V} \sum_{\vec{k}} e^{i\vec{k}(\vec{x}-\vec{x}')} e^{-i\omega_{\vec{k}}(t-t')}$$

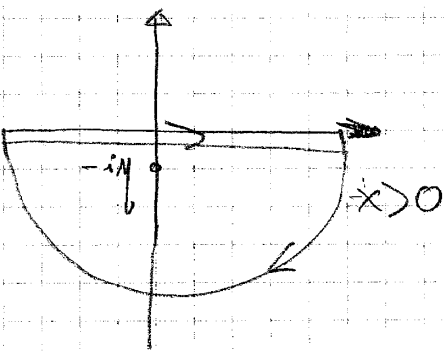
$$[\vartheta(t-t') \vartheta(k - k_F) - \vartheta(t'-t) \vartheta(k_F - k)]$$

Nel limite per volume infinito si ha che:

$$\frac{1}{V} \sum_{\vec{k}} \rightarrow \left(\frac{1}{(2\pi)^3}\right) \int d^3k$$

Rappresentazione integrale della funzione gradino

$$\vartheta(x) = - \int_{-\infty}^{\infty} \frac{dk}{2\pi i} \frac{e^{-ikx}}{k + i\eta}$$



$$\lim_{\eta \rightarrow 0} \left(2\pi i \frac{1}{2\pi i} (k + i\eta) \frac{e^{-ikx}}{(k + i\eta)} \right) = -e^{-\eta x}$$

$$\lim_{\eta \rightarrow 0} (-e^{-\eta x}) = -1 \quad \text{per } x > 0$$

$$= 0 \quad \text{per } x < 0$$

→ direzione del circuito

altro circuito senza poli