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**Calcoli *ab initio* in nuclei medio-pesanti**

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**Lecce**

# CBF FHNC–SOC

$$H = \sum_i \frac{-\hbar^2}{2m_i} \nabla_i^2 + \sum_{i < j} v_{ij} + \sum_{i < j < k} v_{ijk}$$

$$\delta E[\Psi_0] = \delta \frac{\langle \Psi_0 | H | \Psi_0 \rangle}{\langle \Psi_0 | \Psi_0 \rangle} = 0$$

$$\Psi_0(1,2...A) = G(1,2...A)\Phi_0(1,2...A)$$

$$G(1,2...A) = \prod_{i < j} F_{ij}$$

$$F_{ij} = \sum_{p=1,8} f^p(r_{ij}) O_{ij}^p$$

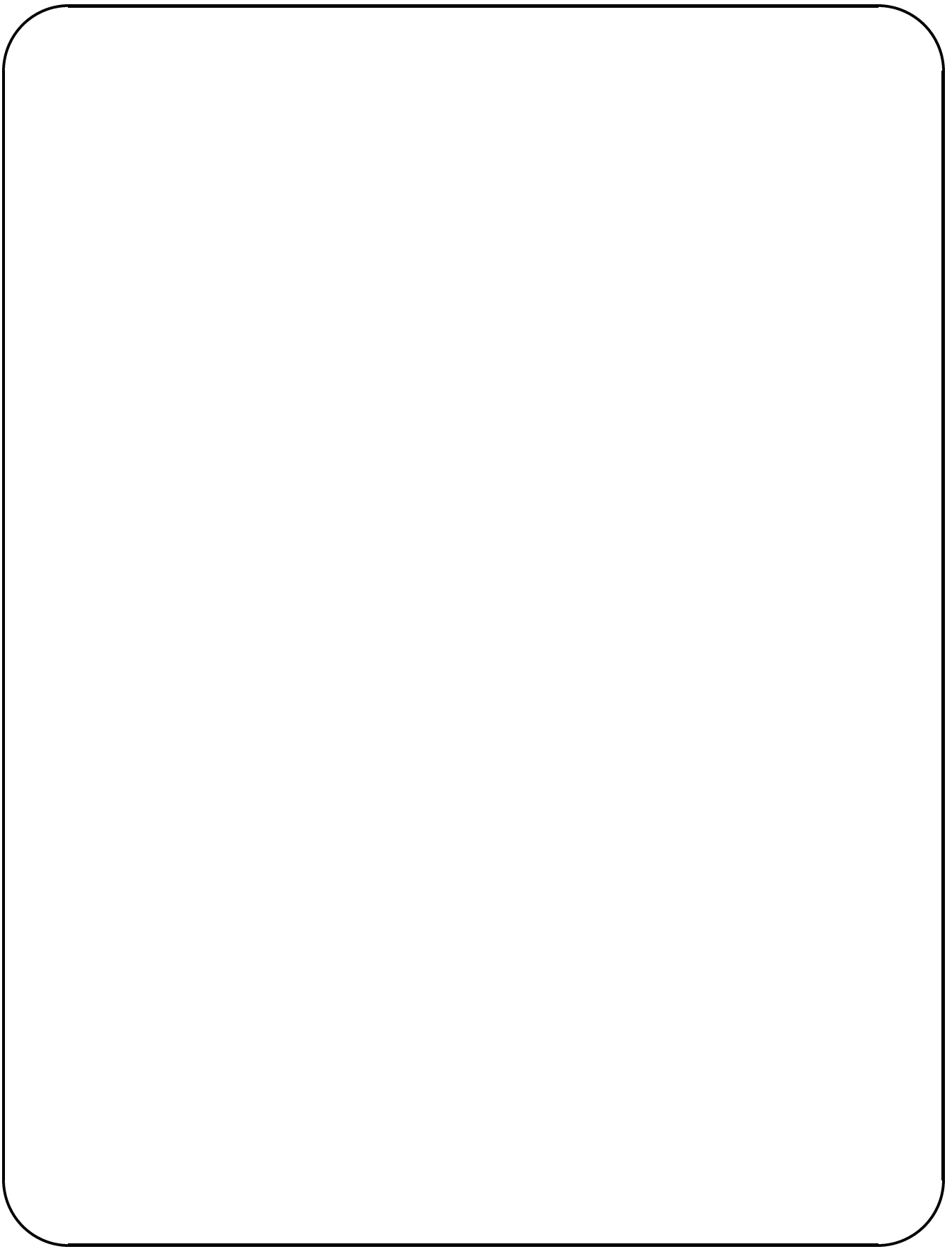
$$O_{ij}^{p=1,8} = [1, \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j, S_{ij}, (\mathbf{L} \cdot \mathbf{S})_{ij}] \otimes [1, \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j]$$

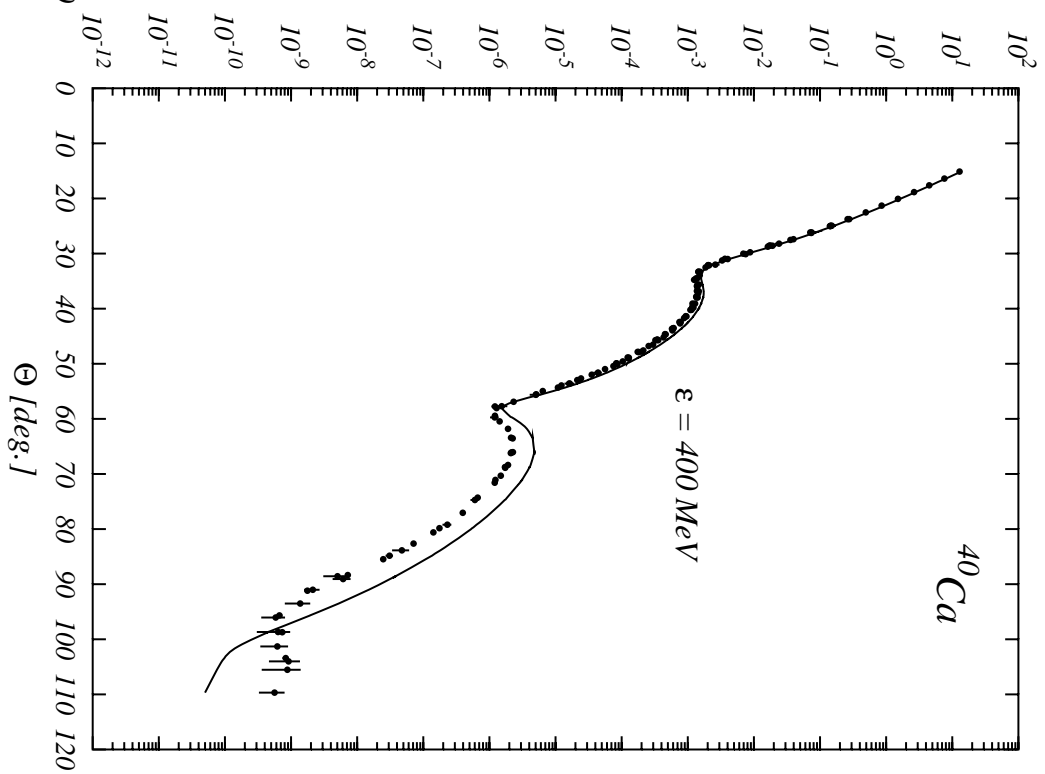
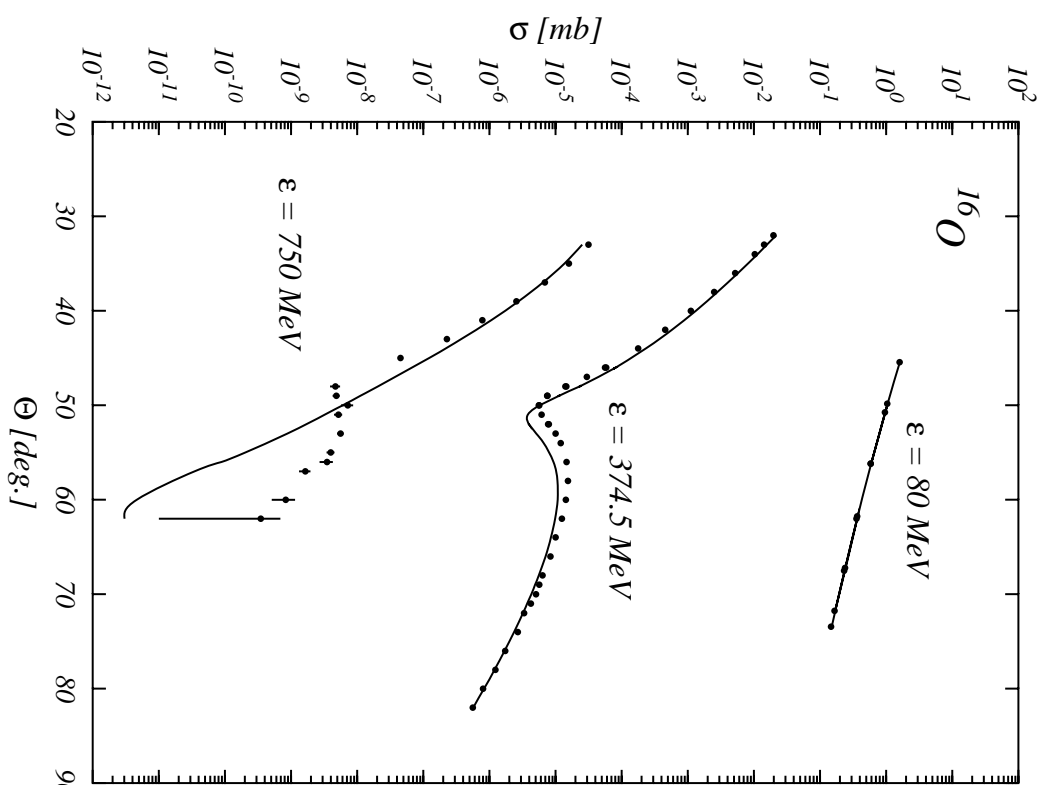
A. Fabrocini, F. Arias de Saavedra and G. C.

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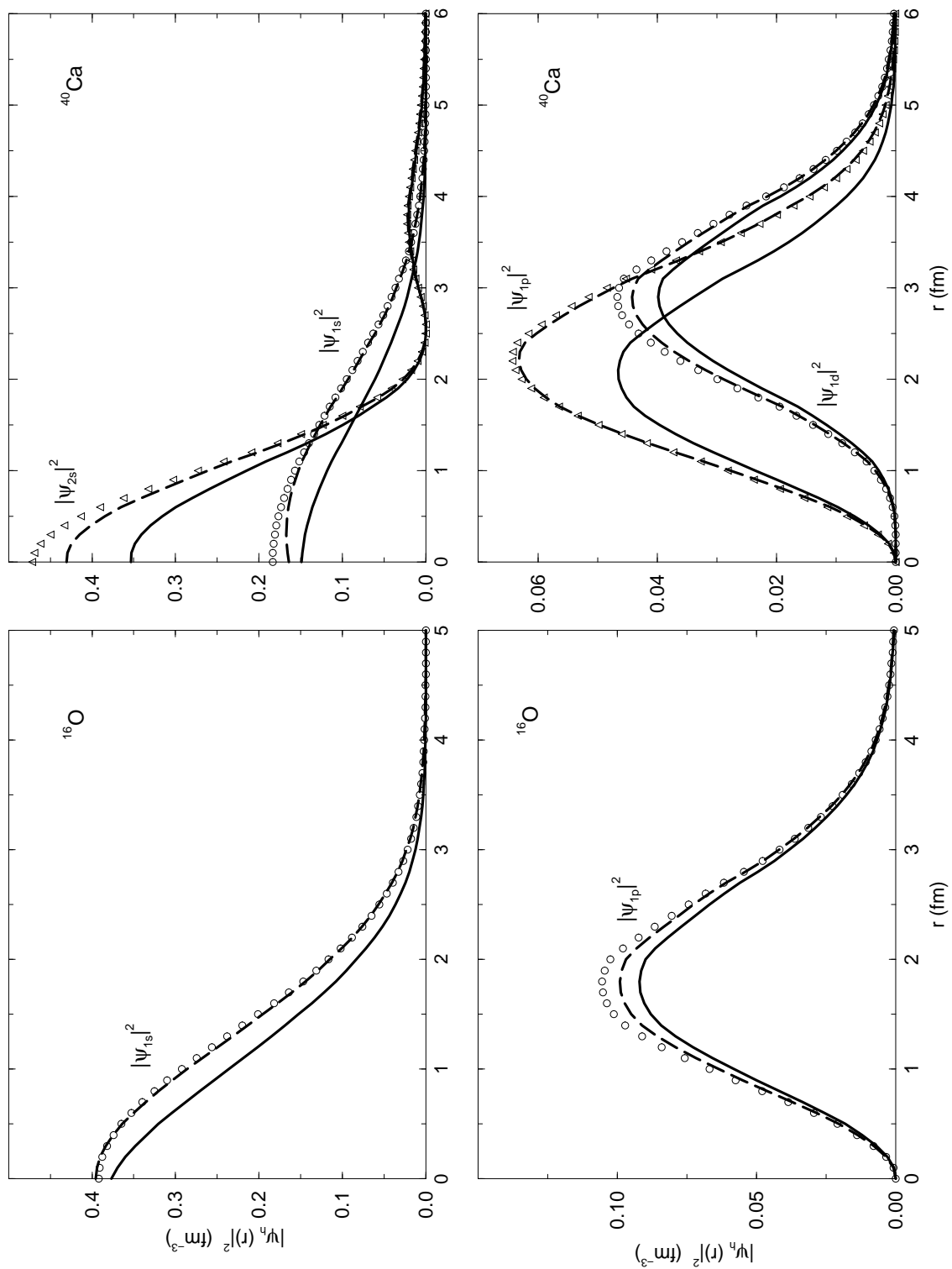
E/A (MeV)	$^{16}\text{O}$	$^{40}\text{Ca}$	n.m.
Exp	-7.97	-8.55	-16.0
A14	-5.11	-6.50	
A8'	-5.48	-6.97	-10.9
A8'*	-5.41	-6.64	

	V [MeV]	R [fm]	a [fm]
$^{16}\text{O}$			
A14	-36.0	3.80	0.55
A8'	-42.0	3.60	0.55
A8'*	-53.0	3.45	0.70
$^{40}\text{Ca}$			
A14	-41.5	5.00	0.55
A8'	-50.0	5.30	0.53
A8'*	-50.0	4.60	0.50





A. Fabrocini and G. C. in preparation.



<sup>16</sup> O	J	<i>f</i> <sub>4</sub>	<i>f</i> <sub>6</sub>
1 <i>s</i>	1.00	0.79	0.70
1 <i>p</i>	0.98	0.96	0.90

<sup>40</sup> Ca	J	<i>f</i> <sub>4</sub>	<i>f</i> <sub>6</sub>
1 <i>s</i>	0.98	0.71	0.55
1 <i>p</i>	0.99	0.76	0.58
1 <i>d</i>	0.97	0.96	0.87
2 <i>s</i>	0.98	0.97	0.86

## Sezioni d'urto

$$\begin{aligned}\sigma(\mathbf{q}, \omega) &\simeq |\langle \tilde{\Psi}_n | O(\mathbf{q}) | \tilde{\Psi}_0 \rangle|^2 \delta(E_n - E_0 - \omega) \\ &\equiv \xi_n^\dagger(\mathbf{q}) \xi_n(\mathbf{q}) \delta(E_n - E_0 - \omega)\end{aligned}$$

$$| \tilde{\Psi}_n \rangle = \frac{|\Psi_n\rangle}{\langle \Psi_n | \Psi_n \rangle^{\frac{1}{2}}}$$

$$\xi_n(\mathbf{q}) = \frac{\langle \Psi_n | O(\mathbf{q}) | \Psi_0 \rangle}{\langle \Psi_n | \Psi_n \rangle^{\frac{1}{2}} \langle \Psi_0 | \Psi_0 \rangle^{\frac{1}{2}}}$$

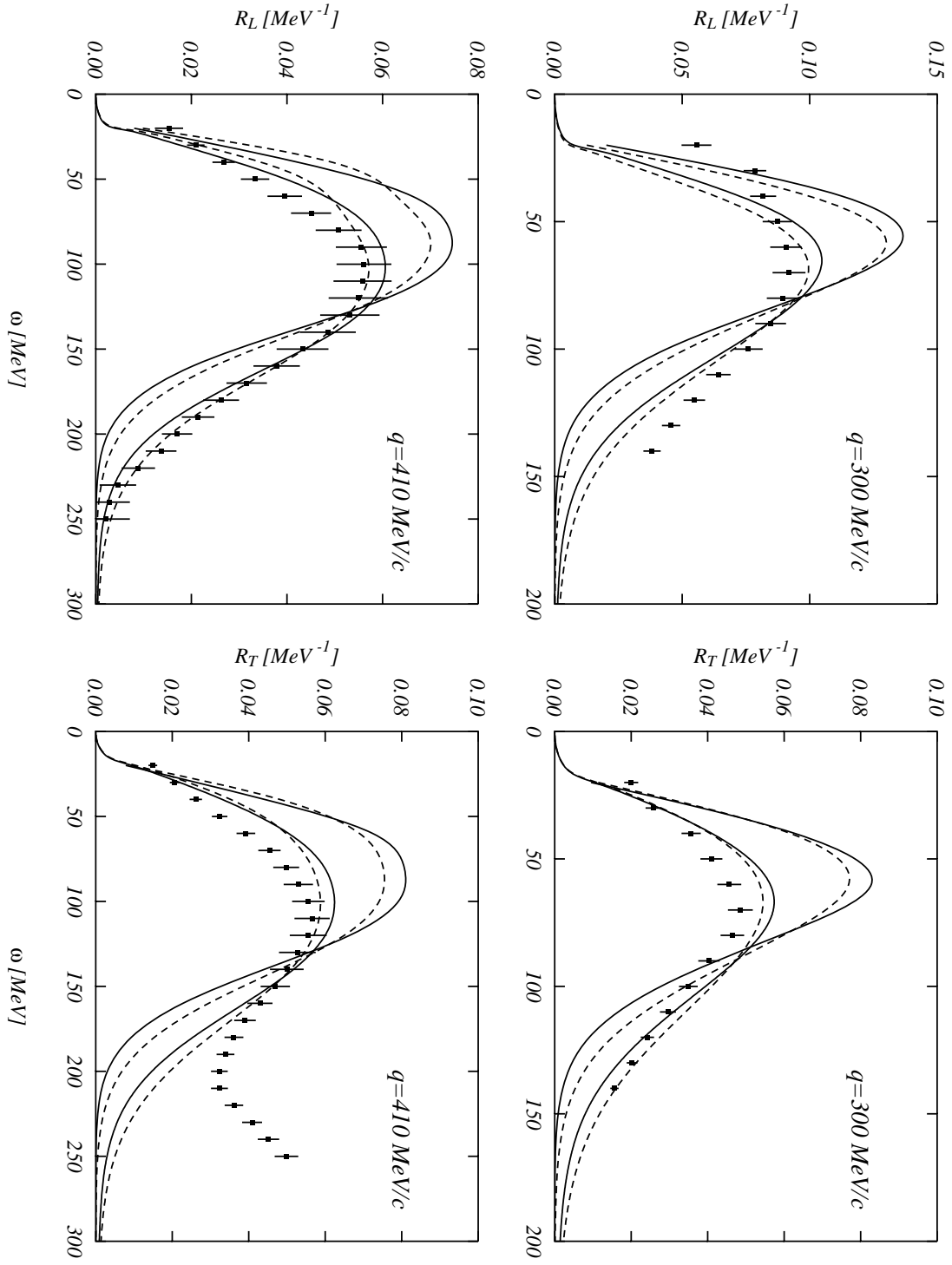
$$|\Psi_0\rangle = G |\Phi_0\rangle \ ; \ |\Psi_n\rangle = G |\Phi_n\rangle$$

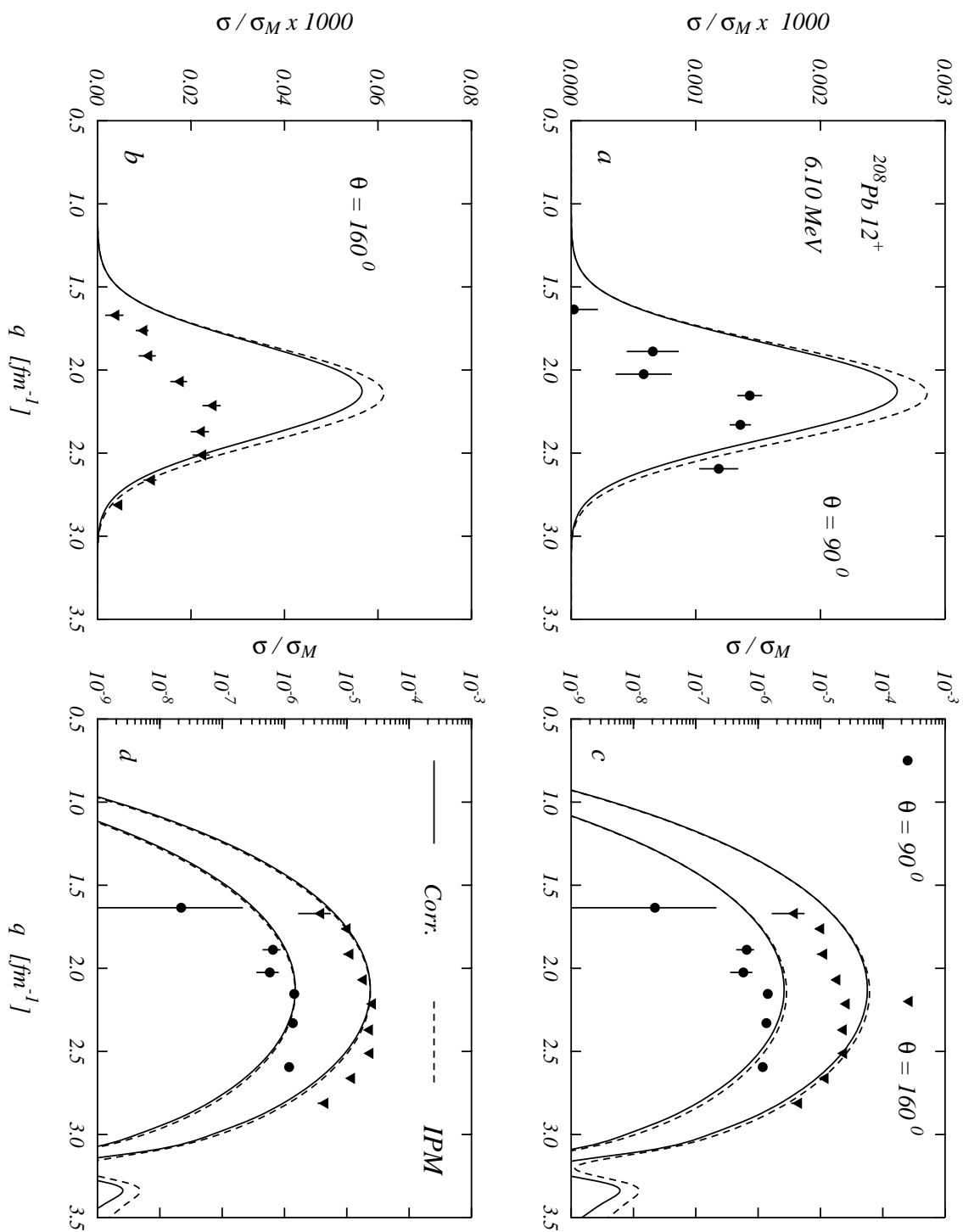
$$\xi_n(\mathbf{q}) = \frac{\langle \Phi_n | G^+ O(\mathbf{q}) G | \Phi_0 \rangle}{\langle \Phi_0 | G^+ G | \Phi_0 \rangle} \left[ \frac{\langle \Phi_0 | G^+ G | \Phi_0 \rangle}{\langle \Phi_n | G^+ G | \Phi_n \rangle} \right]^{\frac{1}{2}}$$

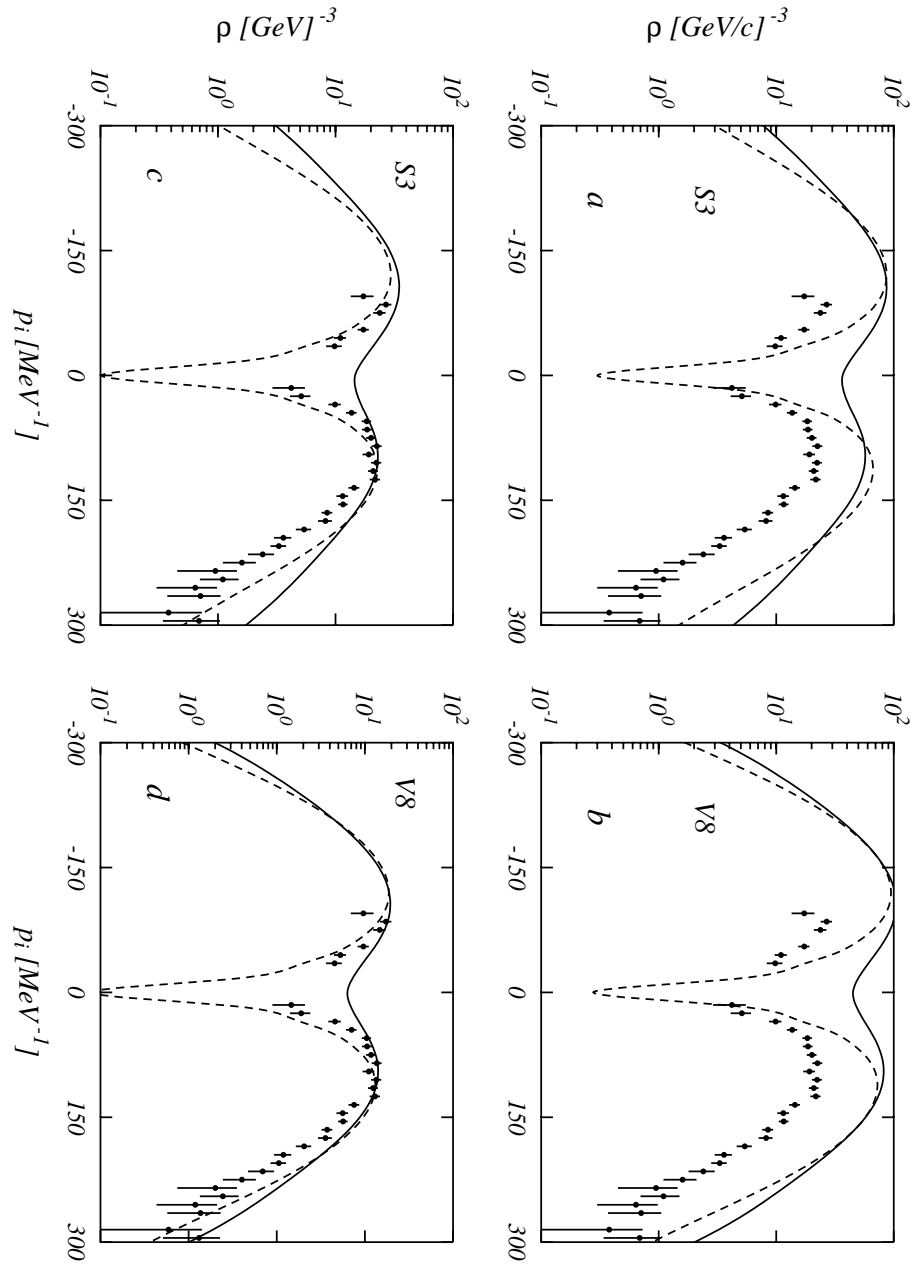


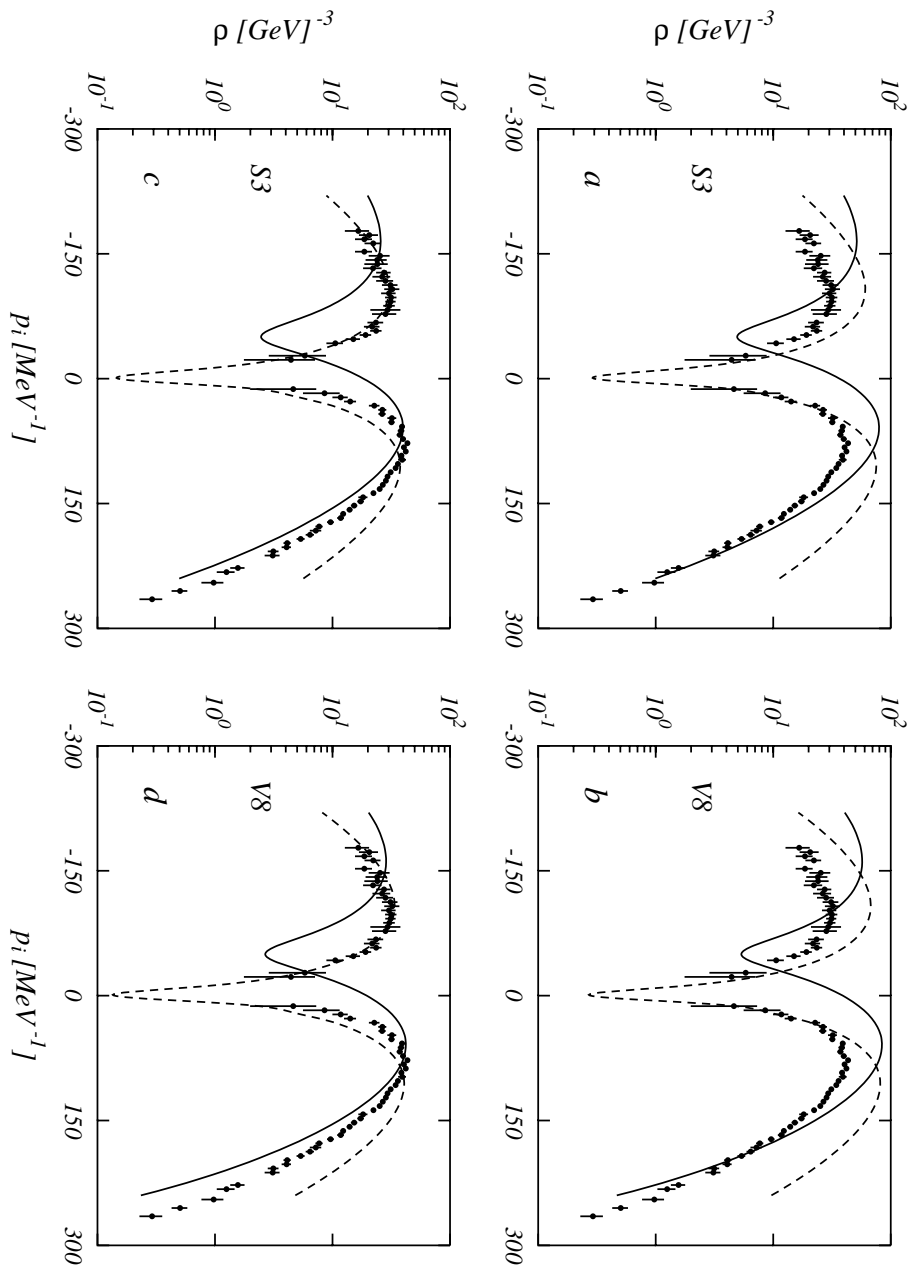
$$\begin{aligned}
& \begin{array}{c} p \quad h \\ \diagdown \quad \diagup \\ \blacksquare \\ (1.1) \end{array} + \frac{1}{2} \left[ \begin{array}{cc} \begin{array}{c} p \quad h \quad i \\ \diagdown \quad \diagup \quad \circlearrowright \\ \blacksquare \quad \cdots \quad \bullet \\ (2.1) \end{array} & - \begin{array}{c} p \quad i \quad h \\ \diagdown \quad \diagup \\ \blacksquare \quad \cdots \quad \bullet \\ (2.2) \end{array} \\ \\ \begin{array}{c} i \quad p \quad h \\ \circlearrowleft \quad \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \blacksquare \\ (2.3) \end{array} & - \begin{array}{c} h \quad i \quad p \\ \diagdown \quad \diagup \\ \blacksquare \quad \cdots \quad \bullet \\ (2.4) \end{array} \end{array} \right] \\
& + \frac{1}{3} \left[ \begin{array}{cc} \begin{array}{c} p \quad k \quad i \\ \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \bullet \\ \quad \quad \quad \diagdown \quad \diagup \\ \quad \quad \quad \blacksquare \\ (3.1) \end{array} & - \begin{array}{c} p \quad k \quad h \\ \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \bullet \\ \quad \quad \quad \diagdown \quad \diagup \\ \quad \quad \quad \blacksquare \\ (3.2) \end{array} \\ \\ \begin{array}{c} h \quad k \quad i \\ \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \bullet \\ \quad \quad \quad \diagdown \quad \diagup \\ \quad \quad \quad \blacksquare \\ (3.3) \end{array} & - \begin{array}{c} h \quad k \quad p \\ \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \bullet \\ \quad \quad \quad \diagdown \quad \diagup \\ \quad \quad \quad \blacksquare \\ (3.4) \end{array} \\ \\ \begin{array}{c} h \quad p \quad i \\ \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \bullet \\ \quad \quad \quad \diagdown \quad \diagup \\ \quad \quad \quad \blacksquare \\ (3.5) \end{array} & - \begin{array}{c} h \quad p \quad i \\ \diagdown \quad \diagup \\ \bullet \quad \cdots \quad \bullet \\ \quad \quad \quad \diagdown \quad \diagup \\ \quad \quad \quad \blacksquare \\ (3.6) \end{array} \end{array} \right]
\end{aligned}$$

G. C. and A.M. Lallena, to be published in Ann. Phys.









## Conclusioni

- ❶ Fattibilità di calcoli *ab initio* per nuclei medio-pesanti.
- ❷ Minimo del funzionale  $E[\Psi_0]$ .
- ❸ Per il confronto con l'esperimento cosa manca?

F. Arias de Saavedra, G. C., A. Fabrocini, in preparation

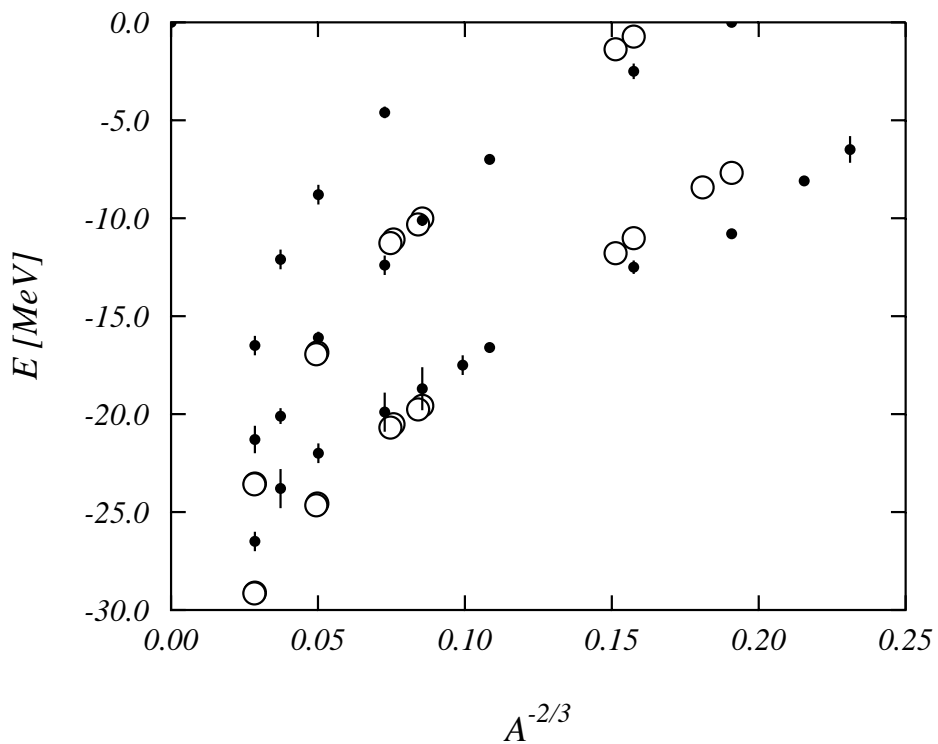
Hypernucleus	$B_{\Lambda}^I$	$B_{\Lambda}^R$	$B_{\Lambda}$
${}_{\Lambda}^{12}\text{C}$	-9.54	1.85	-7.69
${}_{\Lambda}^{13}\text{C}$	-10.16	1.74	-8.42
${}_{\Lambda}^{16}\text{O}$	-12.41	1.39	-11.02
${}_{\Lambda}^{17}\text{O}$	-12.89	1.11	-11.78
${}_{\Lambda}^{40}\text{Ca}$	-20.76	1.18	-19.58
${}_{\Lambda}^{41}\text{Ca}$	-20.84	1.08	-19.76
${}_{\Lambda}^{48}\text{Ca}$	-21.90	1.39	-20.51
${}_{\Lambda}^{49}\text{Ca}$	-22.01	1.32	-20.69
${}_{\Lambda}^{90}\text{Zr}$	-25.88	1.31	-24.57
${}_{\Lambda}^{91}\text{Zr}$	-25.93	1.27	-24.66
${}_{\Lambda}^{208}\text{Pb}$	-30.72	1.60	-29.12
${}_{\Lambda}^{209}\text{Pb}$	-30.74	1.59	-29.15
n.m.	-31.99	1.73	-30.26

Termini di interazione (I) e riarrangemento (R) per l'energia totale della  $\Lambda$  in nello stato S per vari ipernuclei.

Hypernucleus	$B_{\Lambda}^I$	$B_{\Lambda}^R$	$B_{\Lambda}$
$^{16}_{\Lambda}\text{O}$	-1.27	0.54	-0.73
$^{17}_{\Lambda}\text{O}$	-1.74	0.36	-1.38
$^{40}_{\Lambda}\text{Ca}$	-10.73	0.72	-10.01
$^{41}_{\Lambda}\text{Ca}$	-10.97	0.65	-10.32
$^{48}_{\Lambda}\text{Ca}$	-12.32	1.24	-11.08
$^{49}_{\Lambda}\text{Ca}$	-12.45	1.18	-11.27
$^{90}_{\Lambda}\text{Zr}$	-18.13	1.28	-16.85
$^{91}_{\Lambda}\text{Zr}$	-18.20	1.25	-16.95
$^{208}_{\Lambda}\text{Pb}$	-25.28	1.74	-23.54
$^{209}_{\Lambda}\text{Pb}$	-25.31	1.73	-23.58

Termini di interazione (I) e riarrangemento (R) per l'energia totale della  $\Lambda$  in nello stato P per vari ipernuclei.





Dati sperimentali da:

R. Bertini et al. , Phys. Lett. B, **83** (1979) 306.

P.H. Pile et al. , Phys. Rev. Lett. , **66** (1991) 2585.

T. Hasegawa et al. , Phys. Rev. C, **53** (1996) 1210.