

(11)

From the DVR solution we have

$$\psi^{\text{DVR}}(r) = \sum_{\alpha=0}^{N-1} A_{\alpha}^{\text{DVR}} \phi_{\alpha}^{\text{DVR}}(r) + R_0(r) + \mathcal{L}^{\text{DVR}} R_1(r)$$

Then the second order estimate for $\mathcal{L}$ is

$$[\mathcal{L}]^{\text{DVR}} = \mathcal{L}^{\text{DVR}} - \frac{2}{\det(u)} \langle \psi^{\text{DVR}} | H - E | \psi^{\text{DVR}} \rangle$$

The integral

$$\Delta = \langle \psi^{\text{DVR}} | H - E | \psi^{\text{DVR}} \rangle$$

has to be calculated accurately. NOT using quadratures. A tentative to calculate

$$\Delta_q = \sum_{\alpha=0}^{N-1} \psi_{(x_{\alpha})}^{\text{DVR}} [(H - E) \psi^{\text{DVR}}]_{x_{\alpha}}$$

fails to produce a converge result.