

Produzione di particelle come osservabile per l'equazione di stato ad alta densità barionica

Graziella Ferini

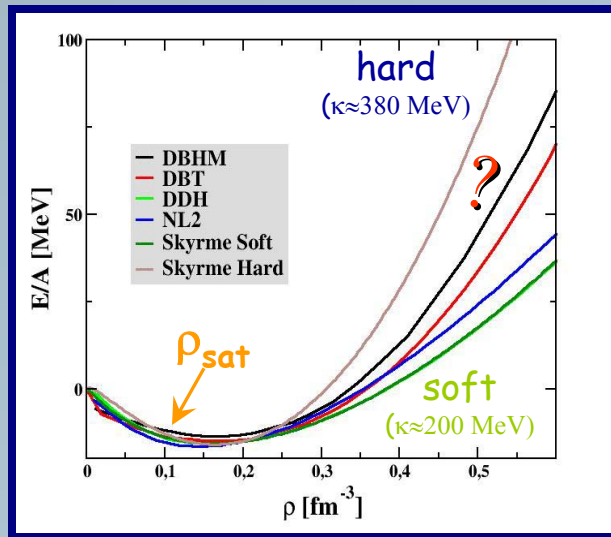
INFN-LNS, Catania

- ✓ Introduzione: l'equazione di stato (EoS)
- ✓ Particelle prodotte in collisioni ad energie relativistiche (1-2 AGeV)
- ✓ Pioni e kaoni come osservabili per l'EoS
- ✓ La fase di alta densità in una reazione ad energie del GeV
- ✓ Conclusioni

Otranto, 29 Maggio-3 Giugno 2006

The Nuclear EOS Uncertainties

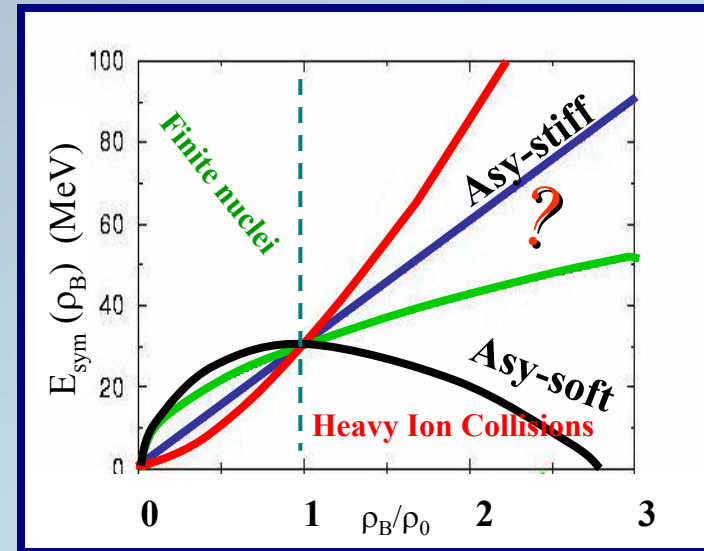
...iso-scalar sector



$$K = 9\rho_0^2 \left(\frac{\partial^2 E}{\partial \rho_B^2} \right) \Big|_{\rho_B = \rho_0}$$

- Particle multiplicity
- Nucleon collective flows (sideward, elliptic) ■

...iso-vector sector



$$\varepsilon_{\text{sym}} \equiv \frac{E_{\text{sym}}}{A}(\rho) = a_4 + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{\text{sym}}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2$$

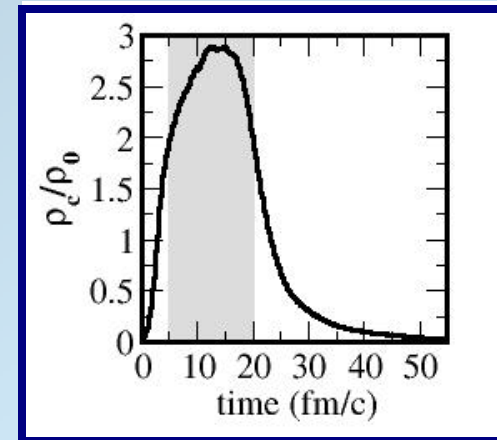
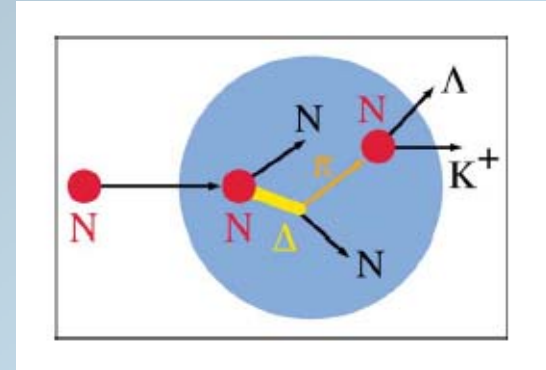
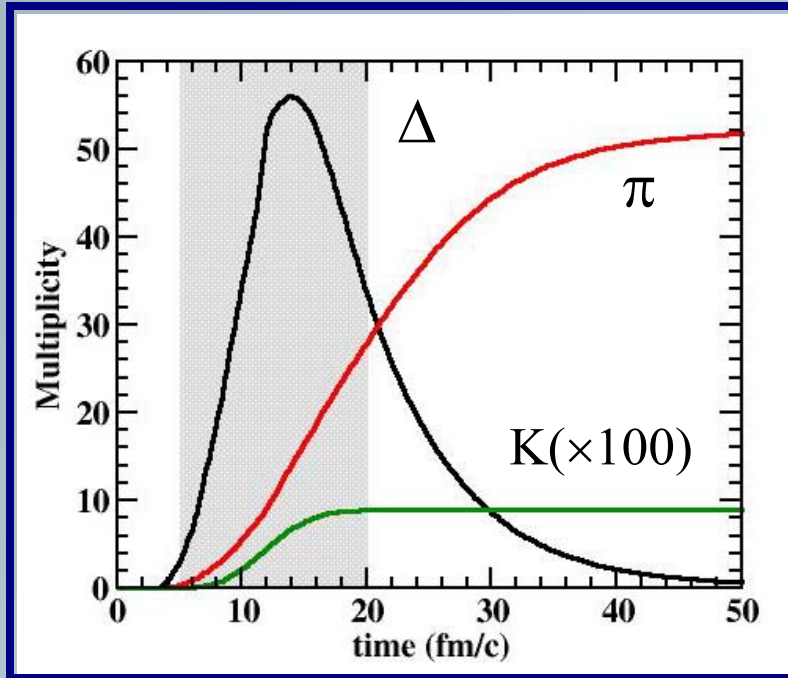
$$L \equiv 3\rho_0 \left(\frac{d\varepsilon_{\text{sym}}}{d\rho} \right)_{\rho=\rho_0} = \frac{3}{\rho_0} P_{\text{sym}}(\rho_0) \quad K_{\text{sym}} \equiv 9\rho_0^2 \left(\frac{d^2\varepsilon_{\text{sym}}}{d^2\rho} \right)_{\rho=\rho_0}$$

Slope parameter

Curvature parameter

- Neutron-proton differential flow
- Isospin equilibration
- Pion flow
- Isospin ratios (π^-/π^+ , K^0/K^+)

Pion and kaon production at GeV energies



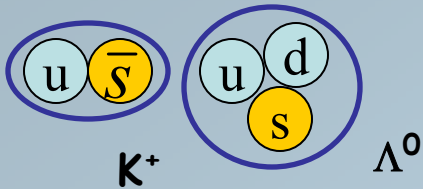
- ✓ pions freeze out late (at low density)
- ✓ kaons freeze out early



K mesons probe the high density phase

Produzione di kaoni

Conservazione di stranezza



- Produzione associata $K + Y$
- $E_{\text{thresh}} \sim 1.56 \text{ AGeV}$
- No riassorbimento per i K
- $\lambda_K \sim 7 \text{ fm}$

$$BB \rightarrow BYK \quad (B \equiv N, \Delta)$$

$$\pi B \rightarrow YK \quad (Y \equiv \Lambda, \Sigma)$$

$$BK \rightarrow BK$$

"emissione diretta"

Produzione sotto soglia:
moto di Fermi + processi "multi-step"

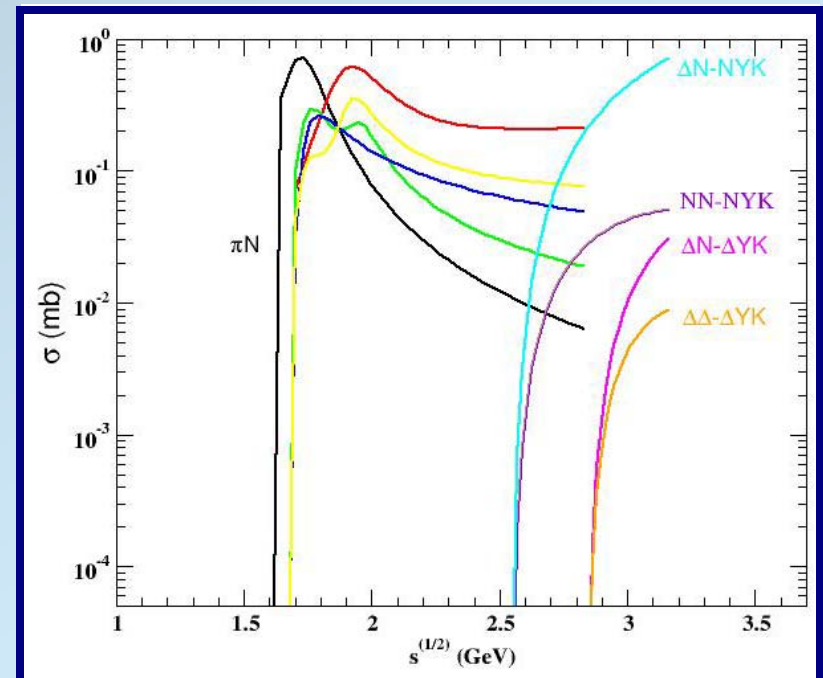


K prodotti ad alta densità

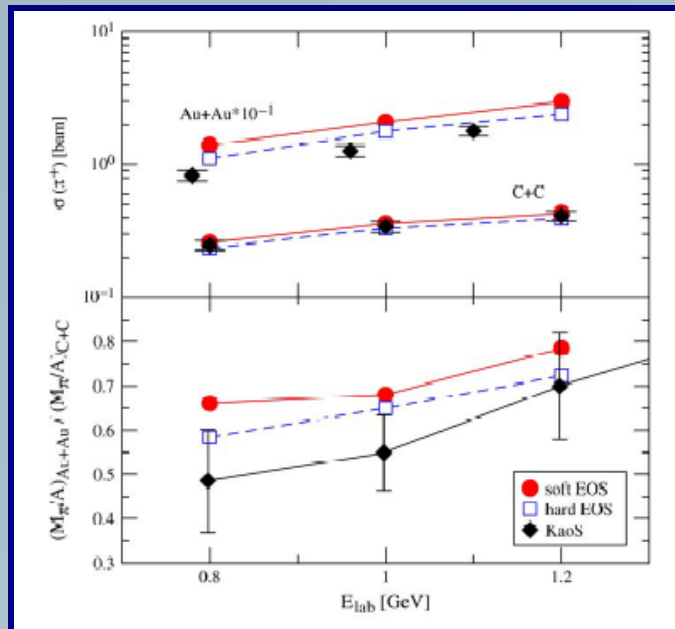
$$\sigma_{BB \rightarrow K} \text{ @ } \sigma_{BB \rightarrow X}$$

Metodo perturbativo: i kaoni non influenzano la dinamica del sistema

$$0.8-2 \text{ AGeV} \Rightarrow \sigma_{BB \rightarrow K} < 1 \text{ mb!}$$



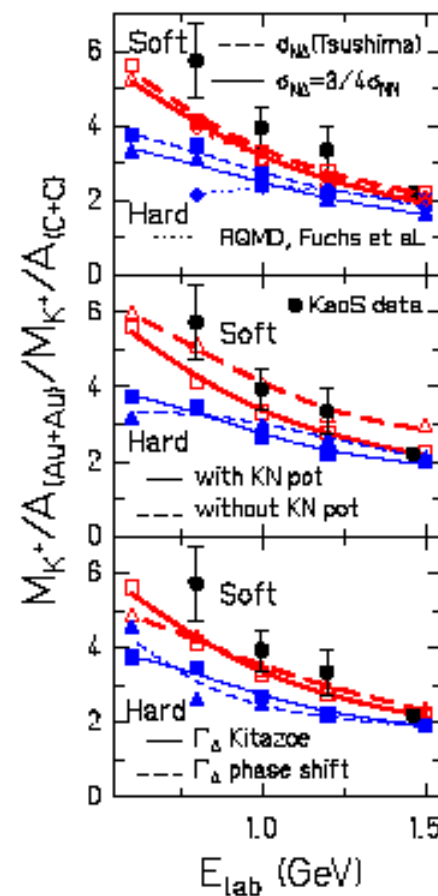
(Isoscalar) EoS from pion and kaon production



π yield does NOT constrain the (isoscalar) EoS

- F. Laue et al. (KaoS Coll.), PRL 82 (1999), 1640.
- C. Sturm et al. (KaoS Coll.), PRL 86 (2001), 39.
- C. Fuchs, Prog. Part. Nucl. Phys. 56 (2006), 1.
- Ch. Hartnack et al., PRL 96 (2006), 012302.

Kaon data only compatible with a soft EoS, even varying:



$N\Delta$ cross section

KN potential

Δ lifetime

Effects of the symmetry energy

$$\Sigma^\mu(p, n) = f_v j^\mu \mp f_s j_3^\mu$$

Baryon current

$$j_{3\mu}(x) = j_\mu^p(x) - j_\mu^n(x)$$

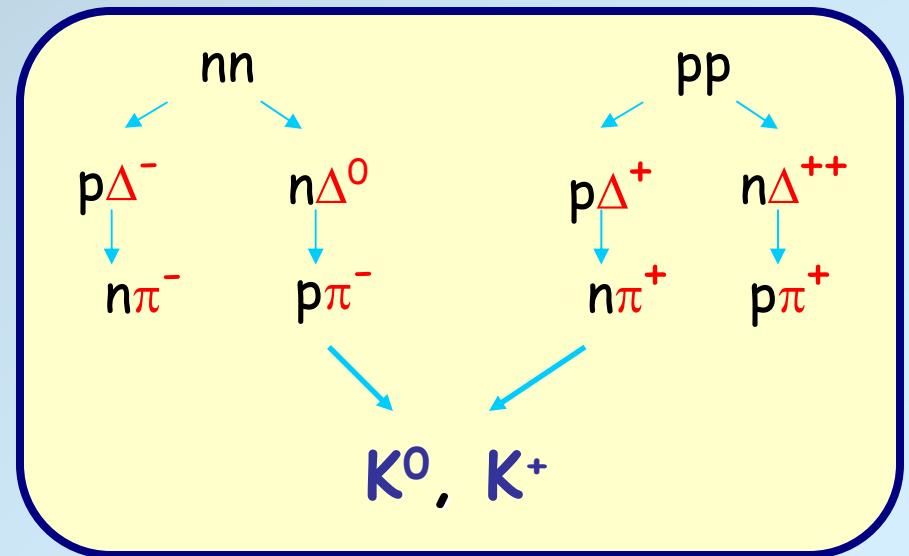
Vector self energy more repulsive for neutrons (-) and more attractive for protons (+)

a) Neutrons pushed out from the high density stage of the reaction

b) Neutrons converted into protons during the high density stage of the reaction

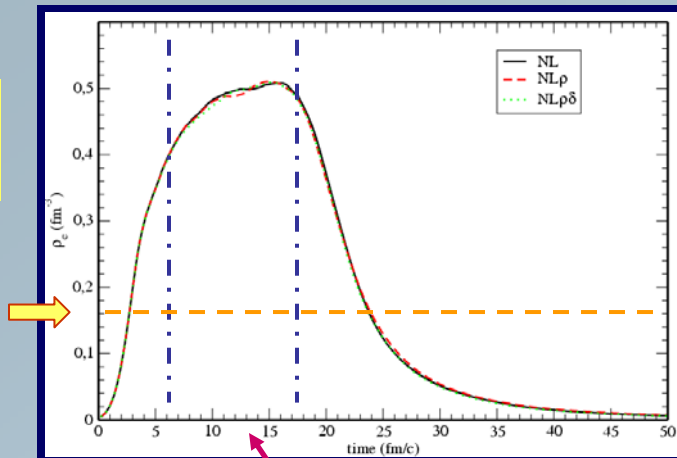
Consequences on

$$\frac{\pi^-}{\pi^+} \quad \text{and/or} \quad \frac{K^0}{K^+} \quad ???$$

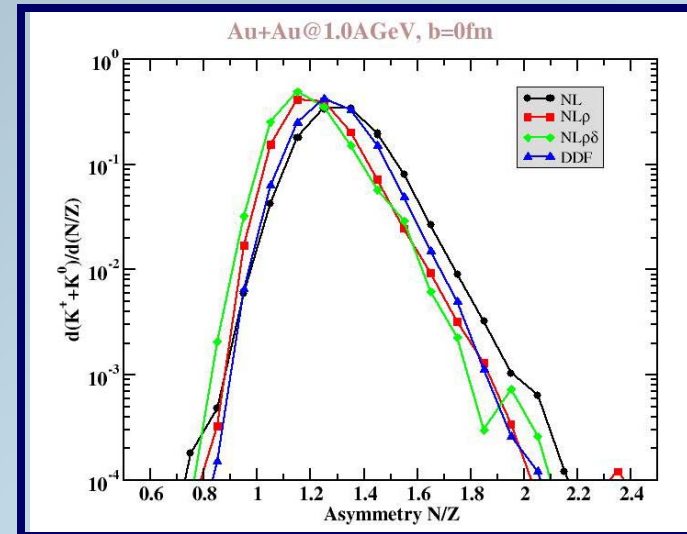


Au+Au 1AGeV: density and isospin of the Kaon source

“central”
density

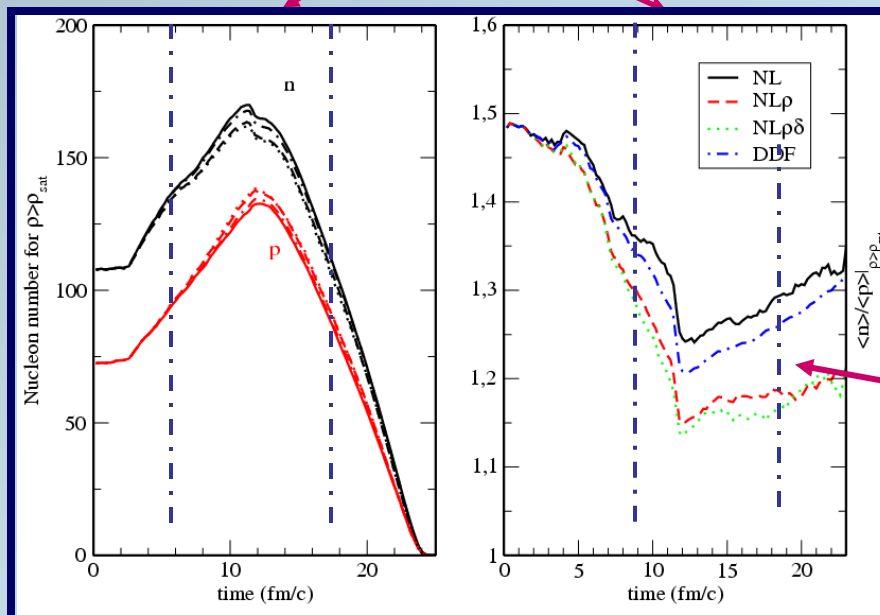


Time interval of Kaon production



NL → DDF → NLρ → NLρδ :
more neutron escape and more n → p
transformation
(less asymmetry in the source)

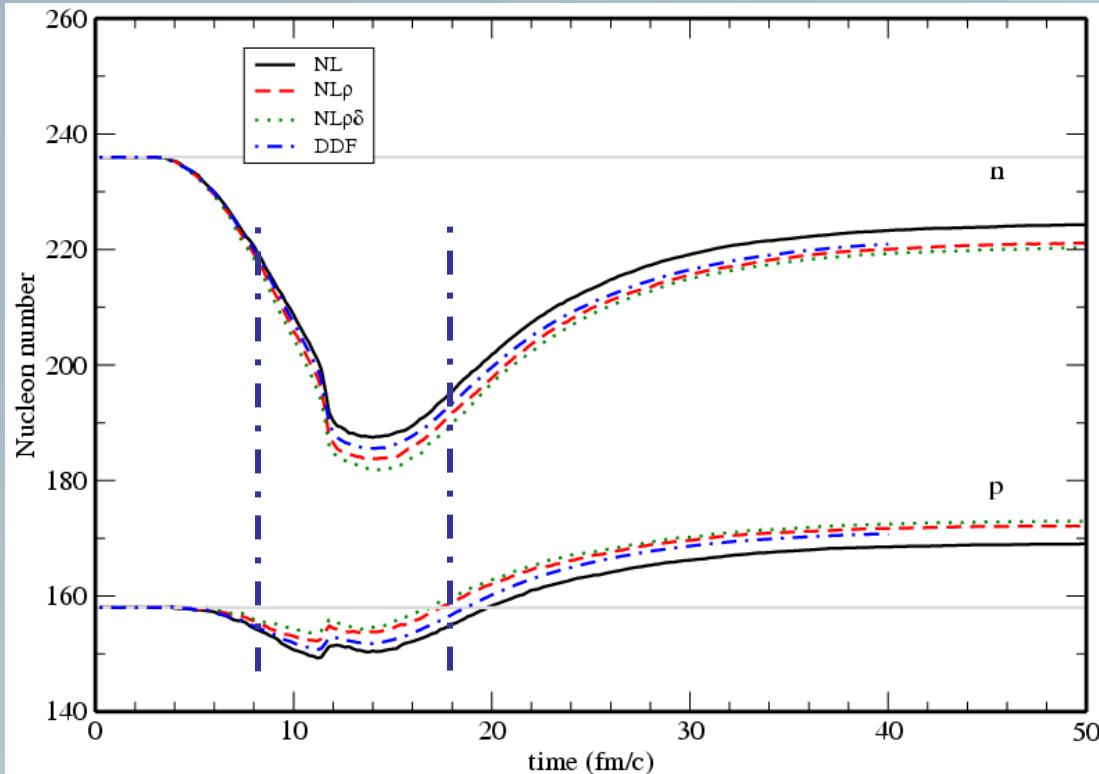
n,p at
High density



n/p at
High density

Drop:
Competition of fast neutron emission
and
Inelastic channels:
n → p transformation

Au+Au@1AGeV: time evolution of the total number of nucleons



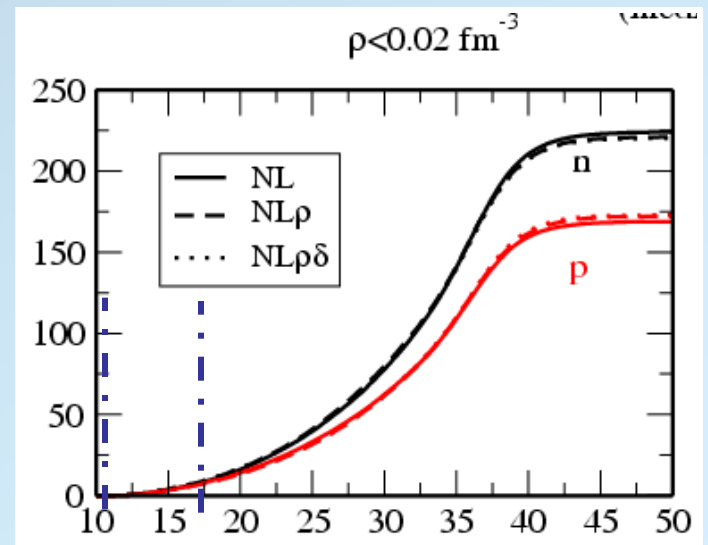
Check:
 π^-/π^+ , n/p , K^0/K^+ vs
 emission time (P_t)

Free nucleons

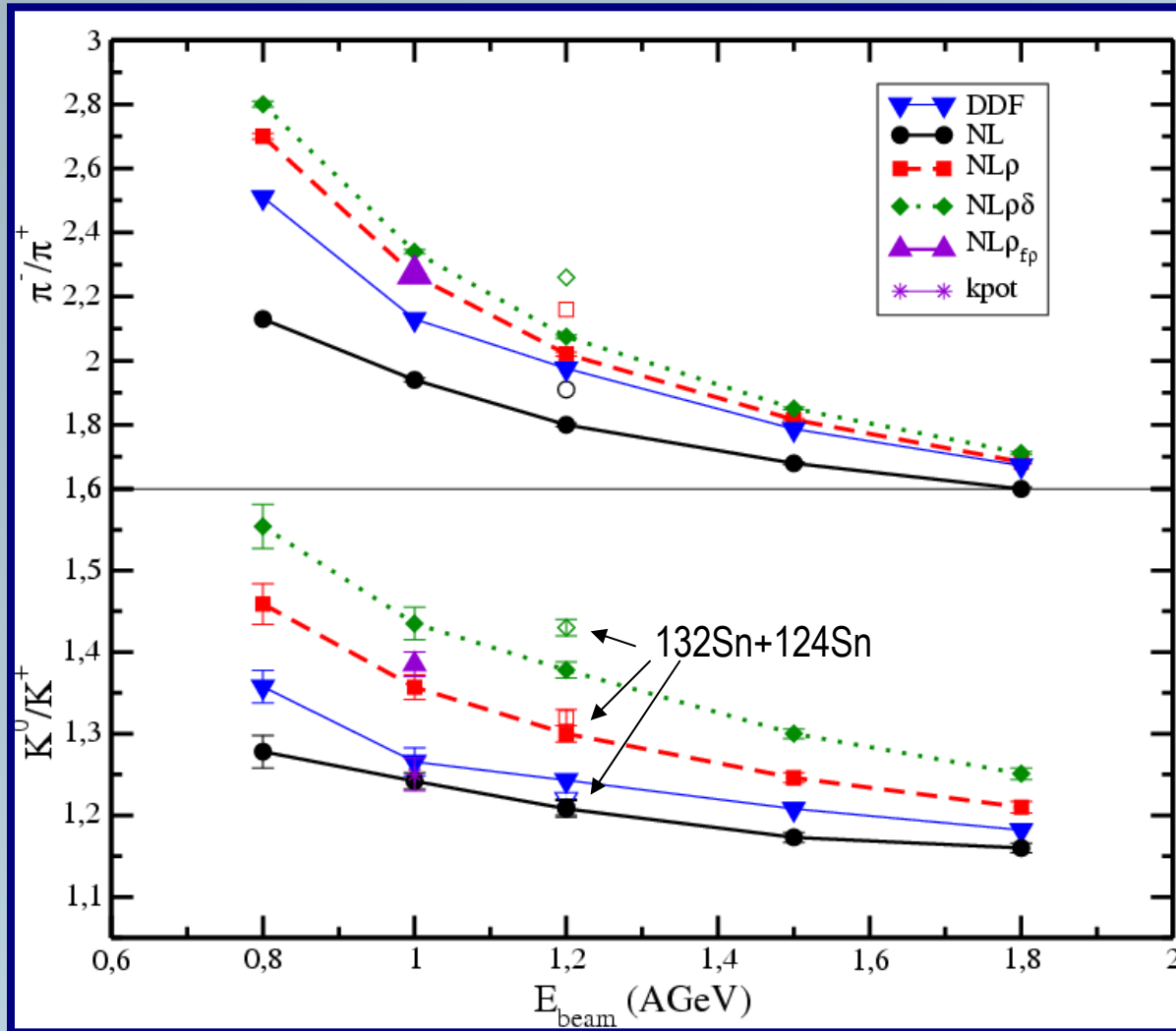
→ Different behavior at lower energies,
 reduced inelastic competition

Large $n \rightarrow p$ transformation
 at early times:
 Less asymmetry in the Kaon source

f_ρ increasing sequence
 $NL < DDF < NL\rho < NL\rho\delta$



Au+Au central: π and K yield ratios vs. beam energy



Kaons:
~15% difference between
DDF and NL $\rho\delta$

No sensitive to
the KN potential

Pions: less sensitivity ~10%, but larger yields

Inclusive multiplicities

Conclusions

➤ Isoscalar sector:

- Nucleon flow data and K^+ multiplicities give indication of a SOFT EoS

➤ Isovector sector:

- E_{sym} reduces the asymmetry in the high density phase of the reaction
- A stiffer E_{sym} (i.e. with greater f_{ρ}) favours the neutron to proton conversion through inelastic collisions
- π^-/π^+ and K^0/K^+ ratios are affected by E_{sym}
- In the 1-2 AGeV range K^0/K^+ ratio is more sensitive to E_{sym} , in terms of the strength of the isovector channel
- The effect is enhanced in colliding systems with large asymmetry

Produzione di K in prossimità della soglia Esperimenti

GSI

FOPI

$^{197}\text{Au}+^{197}\text{Au}$, $^{40}\text{Ca}+^{40}\text{Ca}$,
 $^{96}\text{Ru}(\text{Zr})+^{96}\text{Ru}(\text{Zr})$

- Molteplicità K^+
- Flussi collettivi K^+ , Λ
- K^+ / K^0 per ($\alpha=0.08, 0.16$)

$^{96}\text{Ru}+^{96}\text{Ru}$ @1.5 AGeV

$^{96}\text{Zr}+^{96}\text{Zr}$ @1.5 AGeV

$0.8 < E_{\text{beam}} (\text{AGeV}) < 2$

KaoS

$^{197}\text{Au}+^{197}\text{Au}$, $^{12}\text{C}+^{12}\text{C}$,
 $^{56}\text{Ni}+^{56}\text{Ni}$

- Molteplicità K^+
- Flussi collettivi K^+ , Λ
- Rapporto molteplicità K^+
($^{197}\text{Au}+^{197}\text{Au}$)/($^{12}\text{C}+^{12}\text{C}$)

System size dependence

	N_π/A	N_K/A
$^{40}\text{Ca}+^{40}\text{Ca}$	0.17	1.4×10^{-4}
$^{132}\text{Sn}+^{124}\text{Sn}$	0.14	2.3×10^{-4}
$^{197}\text{Au}+^{197}\text{Au}$	0.13	3.2×10^{-4}

Heavy systems

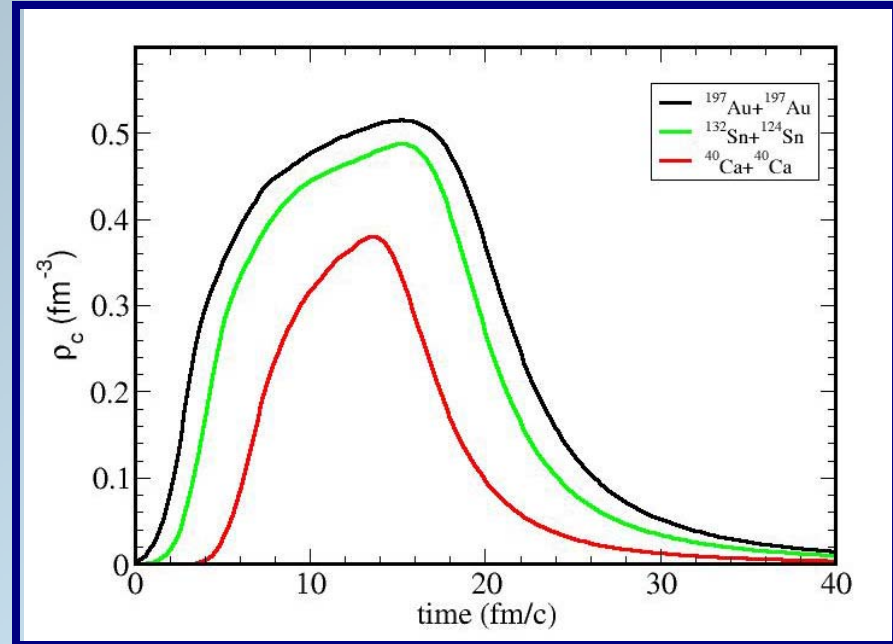


- More collisions
- More stopping
- Higher density



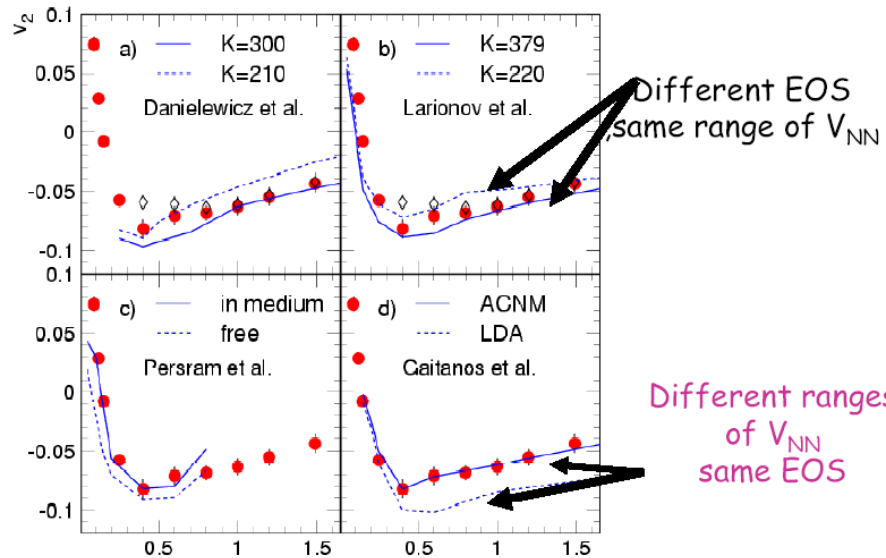
✓ Pions more easily reabsorbed

✓ Kaons more easily produced



Andronic
nucl-ex
0411024

Different
in medium
cross
sections
K=210

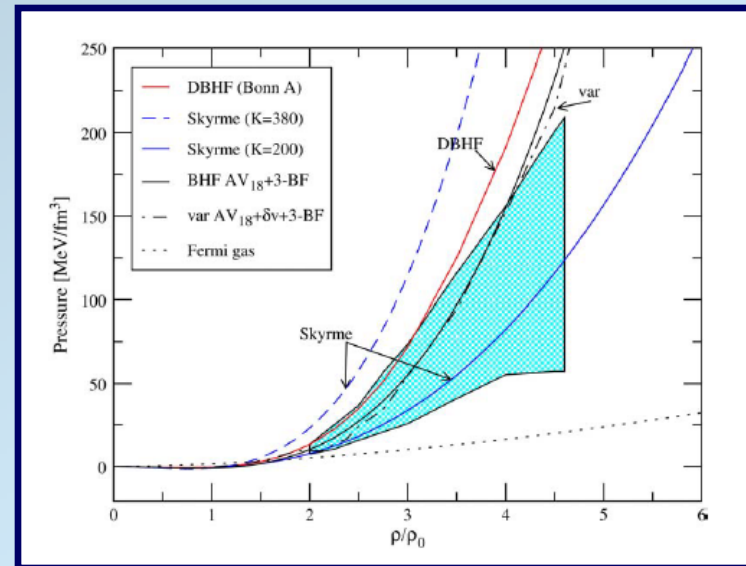


Elliptic flow

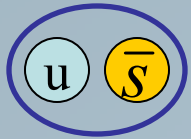
Sideward + elliptic flows
data rule out supersoft
($K=167$ MeV) and hard
($K>300$ MeV) EoS



Soft EoS
($K \approx 200$ MeV)



I kaoni: generalità

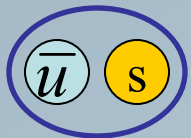


K^+

$$K^+ \rightarrow \mu^+ + \nu_\mu,$$

$$K^+ \rightarrow \pi^+ + \pi^0$$

$\left. \vphantom{\begin{matrix} K^+ \rightarrow \mu^+ + \nu_\mu \\ K^+ \rightarrow \pi^+ + \pi^0 \end{matrix}} \right\} (\tau \sim 1 \times 10^{-8} \text{ s})$



K^-

$$K^- \rightarrow \mu^- + \bar{\nu}_\mu,$$

$$K^- \rightarrow \pi^- + \pi^0$$

K^0 è una combinazione di coppie $d\bar{s}$ e $\bar{d}s$ e può decadere in 2 modi:

$$K^0_S \rightarrow \pi^+ + \pi^-$$

$$K^0_S \rightarrow \pi^0 + \pi^0$$

$(\tau \sim 9 \times 10^{-11} \text{ s})$

$$K^0_L \rightarrow \pi^+ + \pi^- + \pi^0$$

$$K^0_L \rightarrow \pi^0 + \pi^0 + \pi^0$$

$(\tau \sim 5 \times 10^{-8} \text{ s})$

massa

$$\left\{ \begin{array}{l} m_{K^+} = m_{K^-} \approx 494 \text{ MeV}/c^2 \\ m_{K^0} \approx 498 \text{ MeV}/c^2 \end{array} \right.$$

Il potenziale e gli effetti del mezzo sui kaoni

Effetti osservabili:

- ✓ Distribuzione azimutale
- ✓ Flusso trasverso
- ✓ Soglia di produzione

Approcci:

- ✓ CPT (Chiral Perturbation Theory)
- ✓ BEM (Boson Exchange Model)

Relazioni di dispersione:

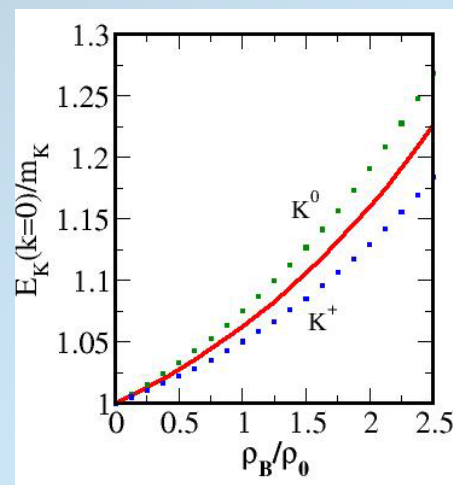
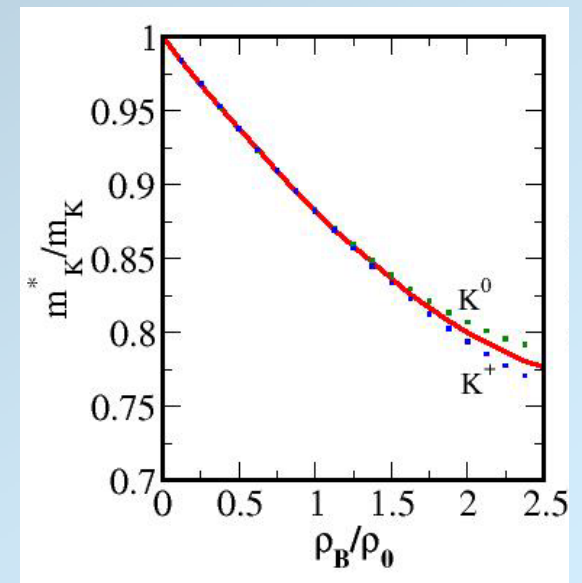
$$\omega_{K^+} = \left[m_K^2 + k^2 - g_{\sigma K} m_K \phi + (g_{\omega K} V_0)^2 \right]^{1/2} + g_{\omega K} V_0$$

$$\omega_{K^-} = \left[m_K^2 + k^2 - g_{\sigma K} m_K \phi + (g_{\omega K} V_0)^2 \right]^{1/2} - g_{\omega K} V_0$$

Massa efficace:

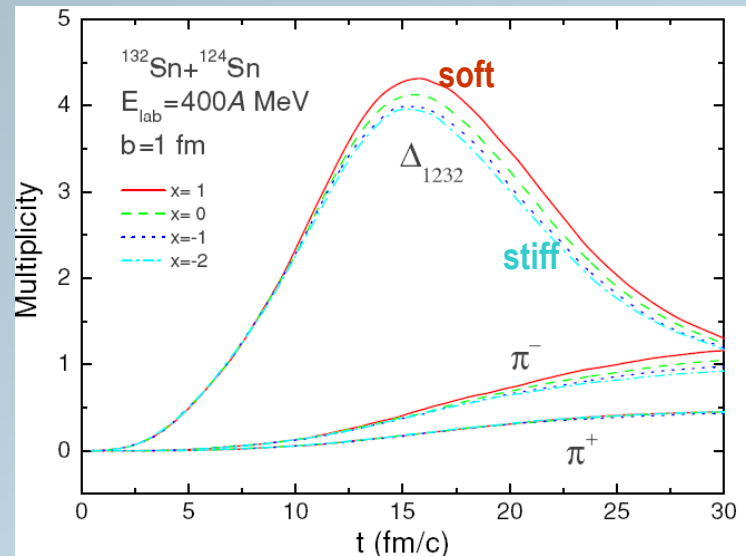
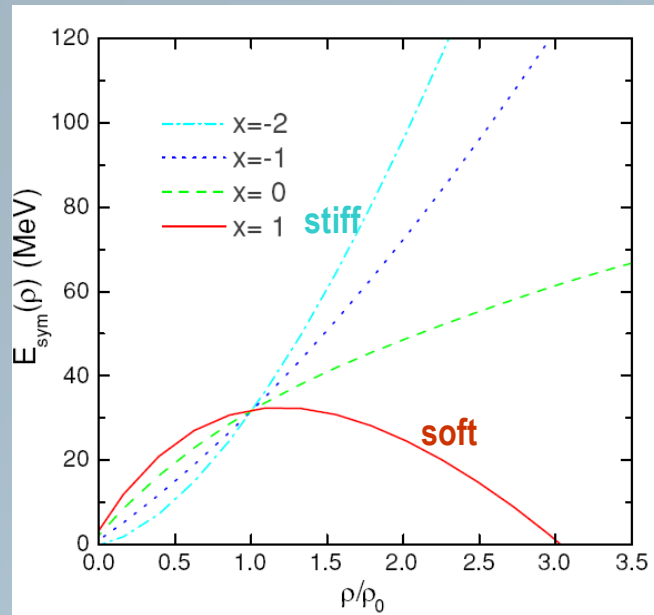
$$m_{k^{+,-}}^* = \sqrt{\left(m_k^2 - \frac{\Sigma_{KN}}{f_\pi^2} \rho_s + V_\mu V^\mu \right)}$$

$$V_\mu = \frac{3}{8f_\pi^2} j_\mu$$

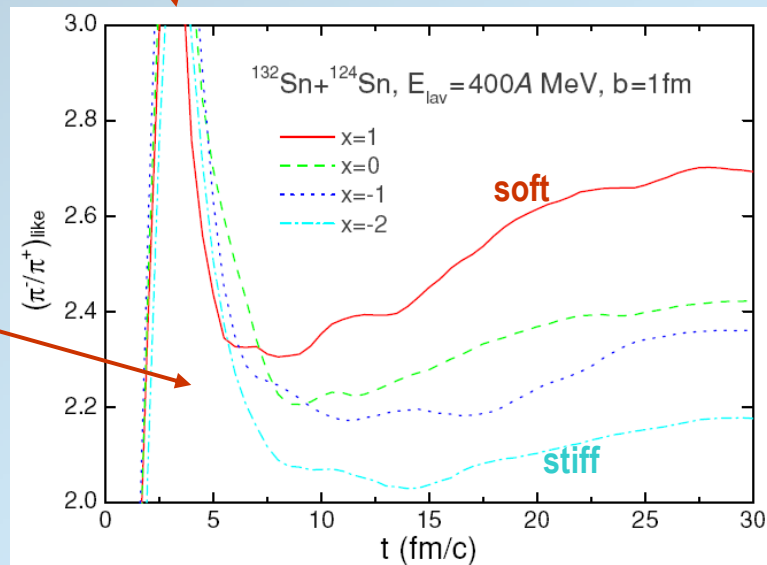


IBUU : not covariant symmetry term

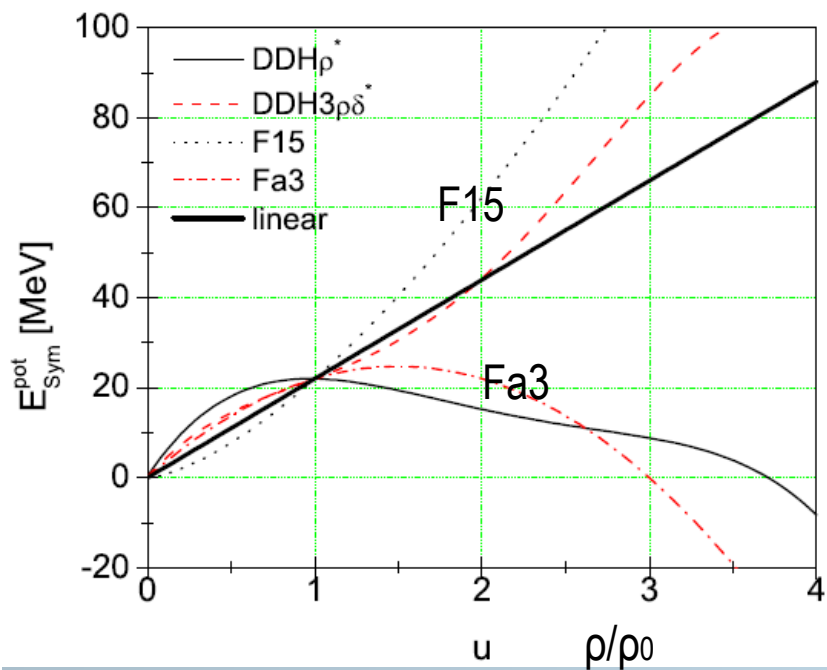
$^{132}\text{Sn}+^{124}\text{Sn}$ at 0.4A GeV



fluctuations

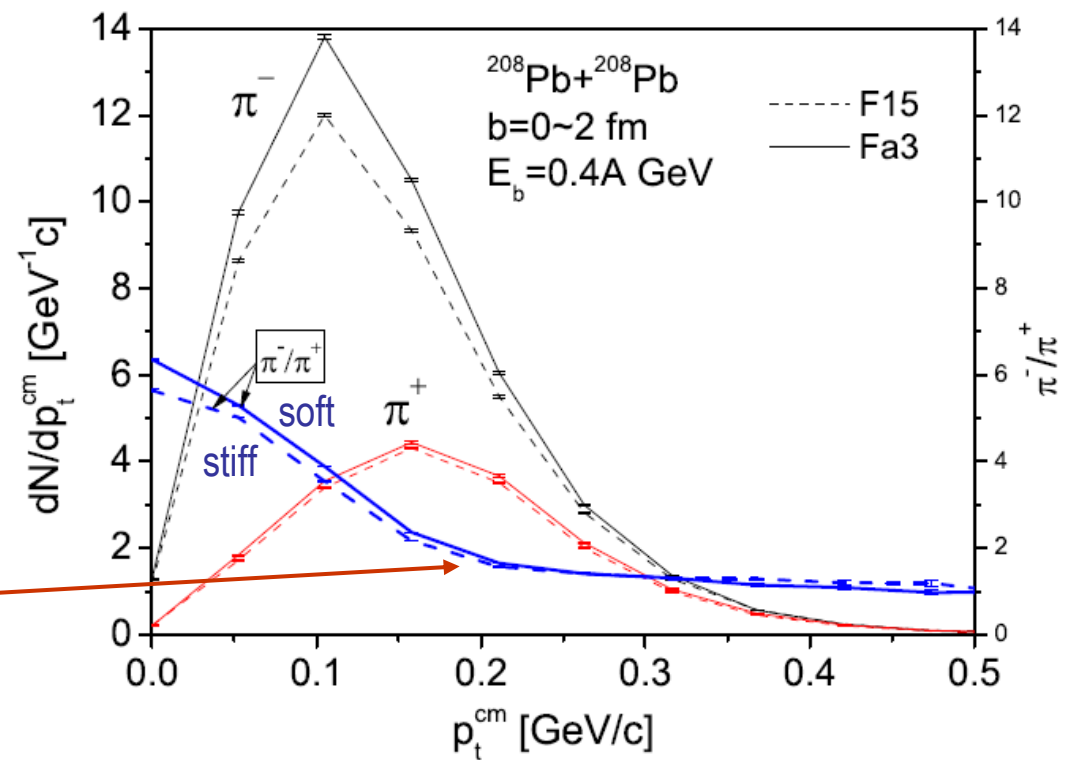


$\pi(-)/\pi(+)$ always decreasing with the iso-stiffness?

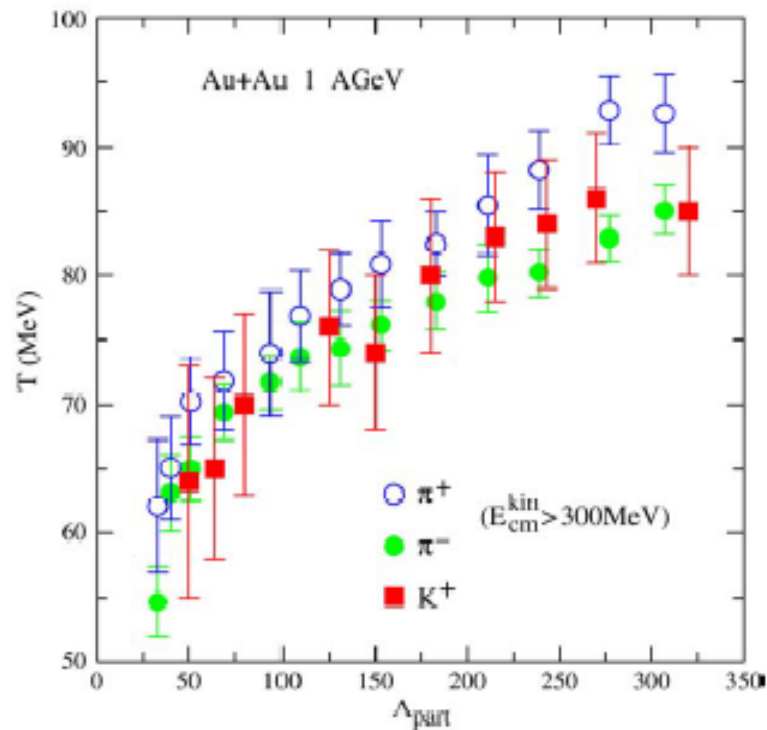


UrQMD : not covariant symmetry term

208Pb+208Pb at 0.4A GeV



Inelastic channels less important
but still crossing at high p_t



Kaons behave
like high
energy pions

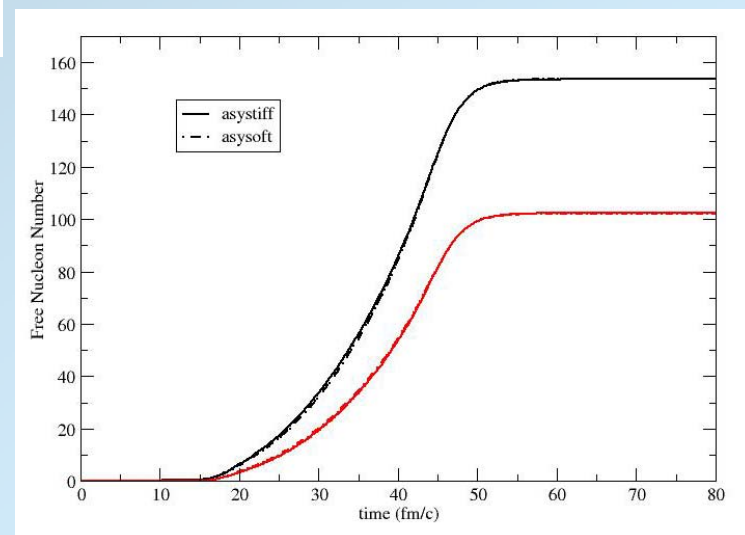
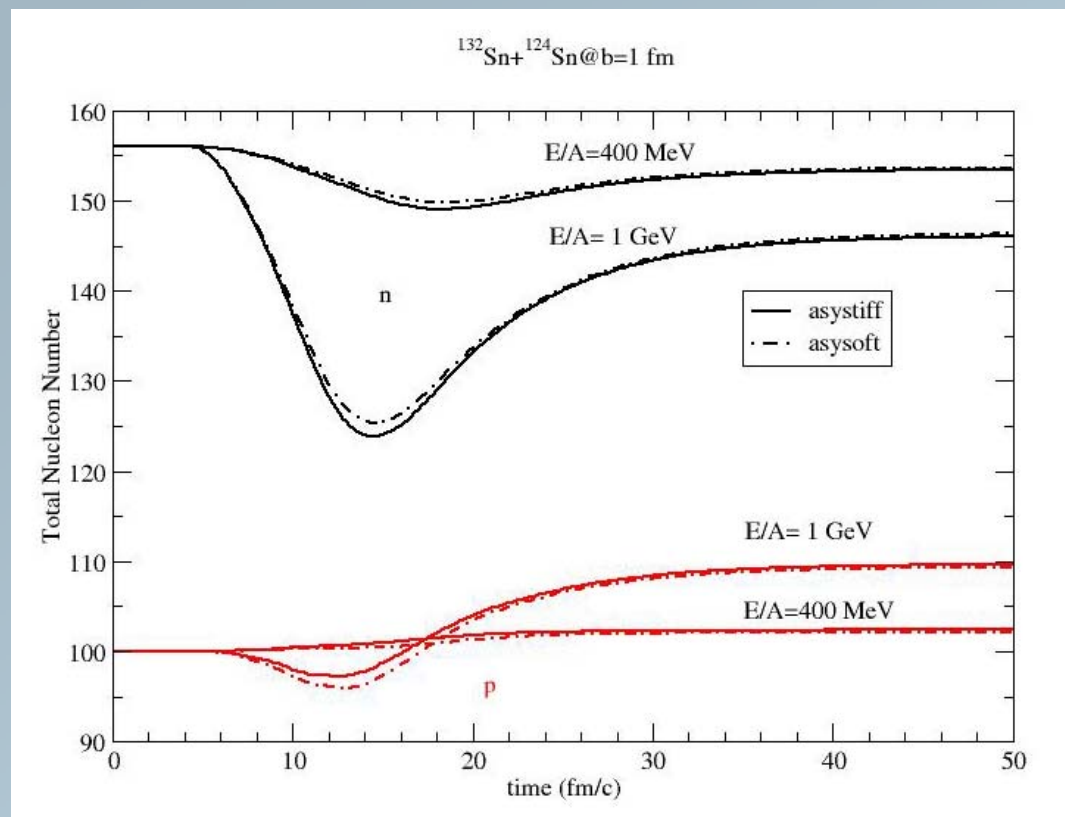
P. Senger, H. Stroebele, J. Phys. G 25 (1999) R59

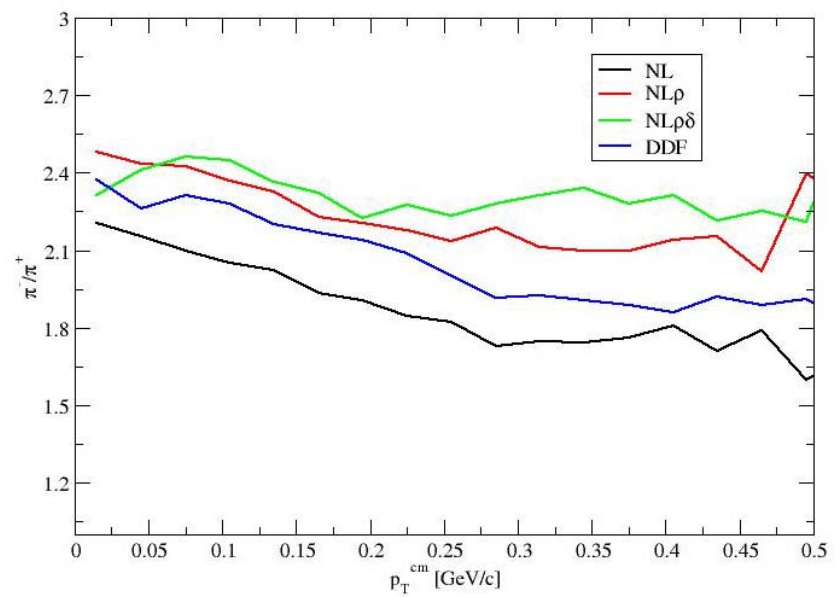
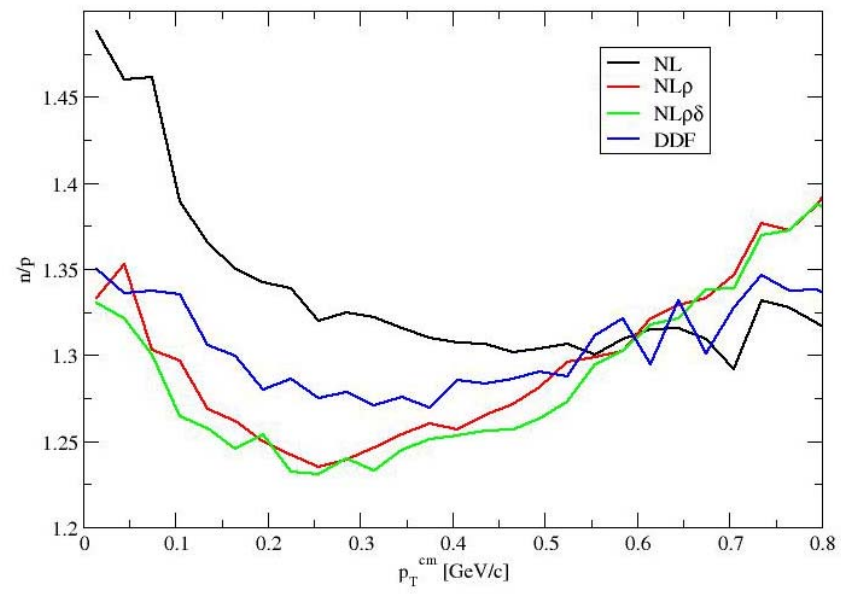
D Best et al, Fopi, NPA 625 (1997), 307

Bass et al, PRC 51 (1995), 3343

Wagner et al, kaos, PLB 420 (1998), 20

Wagner et al., kaos, PRL 85 (2000), 18



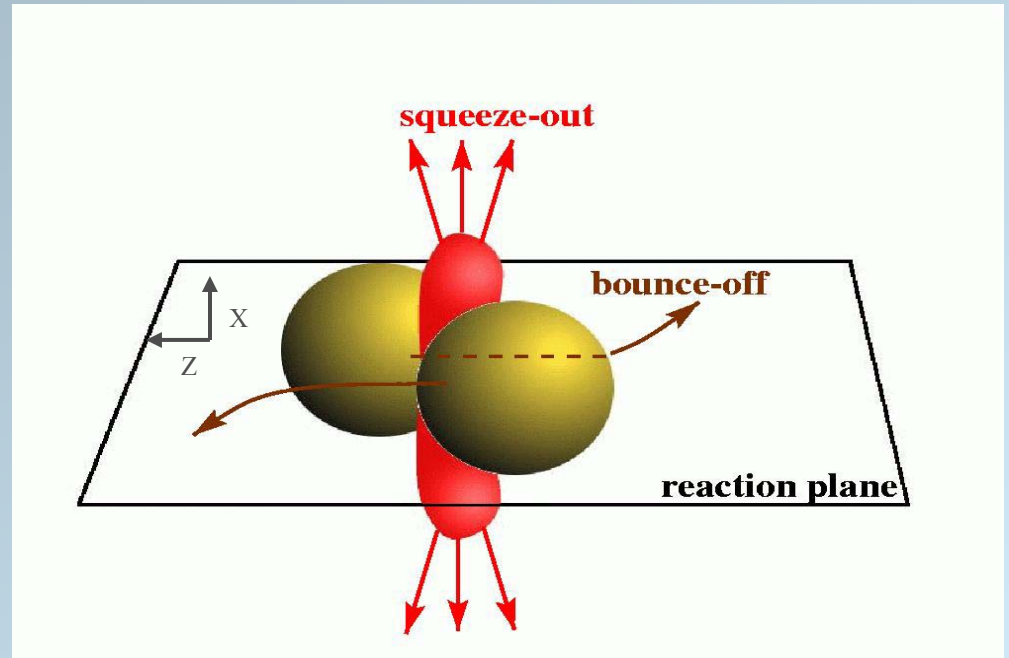


$$\langle p_x(y) \rangle = \frac{1}{N(y)} \sum_i p_{xi}(y)$$

Bounce-off
(in-plane flow)

$$V_2(p_t) = \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle$$

Squeeze-out
(elliptic flow)



$$F^{p-n}(y) = \frac{1}{N(y)} \sum_i p_{xi}(y) \tau_i \quad \leftarrow$$

Isospin



$$V_2^{p-n}(p_t) = V_2^p(p_t) - V_2^n(p_t)$$

Differenze tra $NL\rho$ e $NL\rho\delta$

(V. Greco et al., PLB 562 (2003), 215)